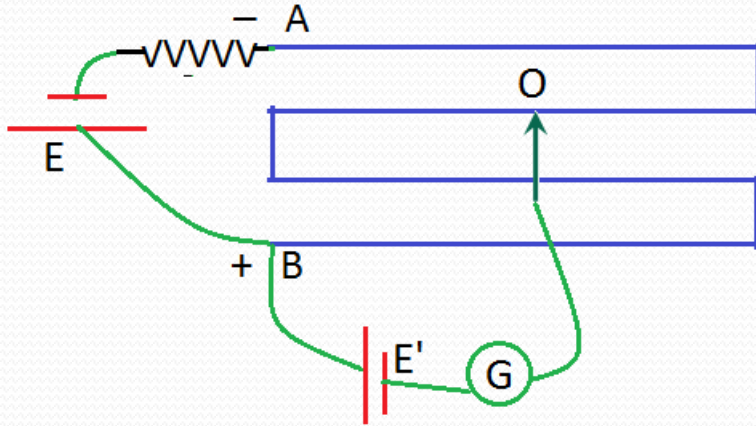


$$AB = L, R_L = R$$



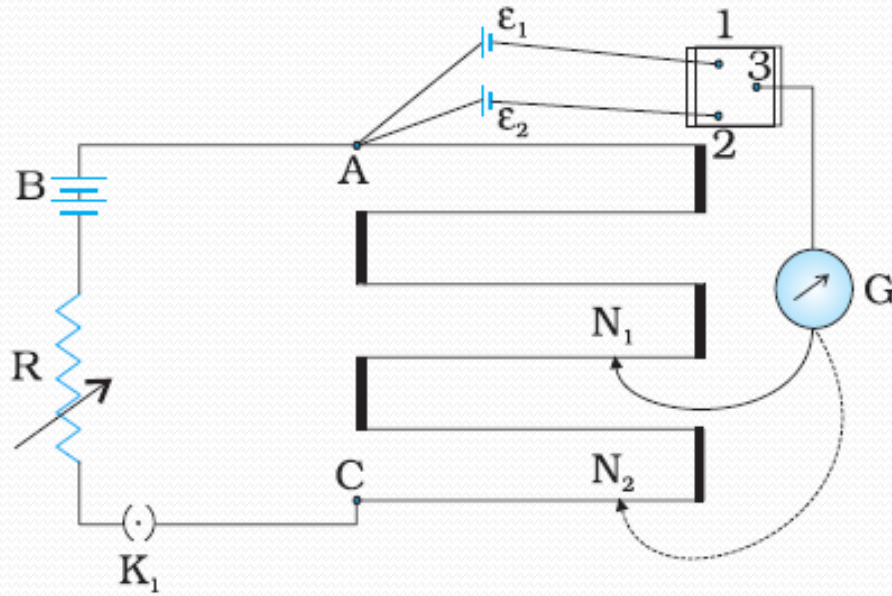
$$E' = V_{BO} \text{ Galvanometer } I' = 0$$

$$I = \frac{E}{R} = \frac{E}{\rho \frac{L}{A}} = \frac{EA}{\rho L}$$

$$V_1 = IR_1 = I\rho \frac{l}{A}$$

$$V_1 \propto l \Rightarrow V_1 = kl$$

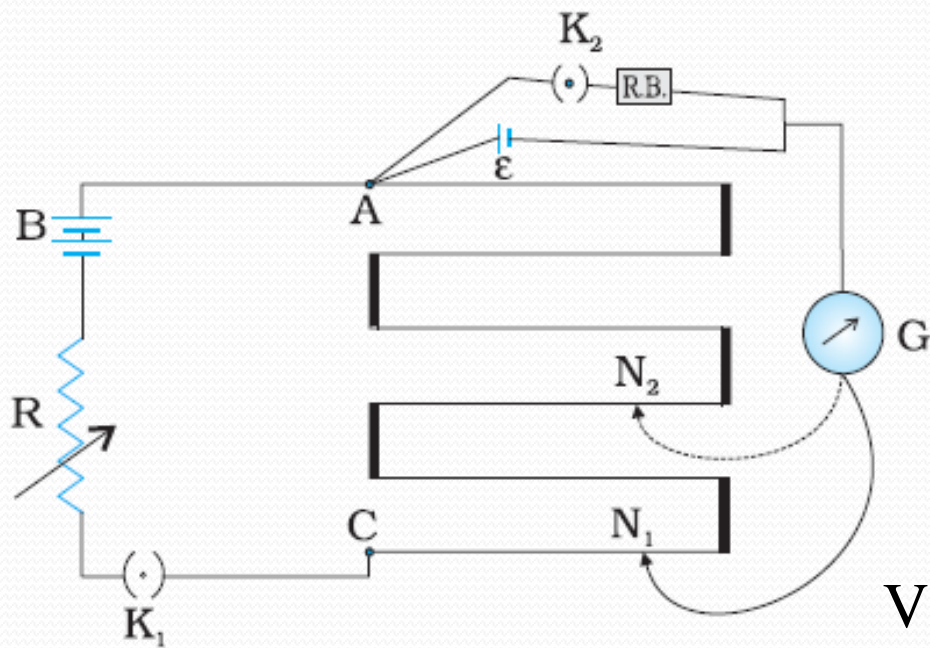
$$V_{BO} = IR_{BO} = I\rho \frac{l_{BO}}{A}$$



$$E_1 = kl_1 = kl_{AN_1}$$

$$E_2 = kl_2 = kl_{AN_2}$$

$$\frac{E_1}{E_2} = \frac{kl_1}{kl_2} = \frac{l_1}{l_2}$$



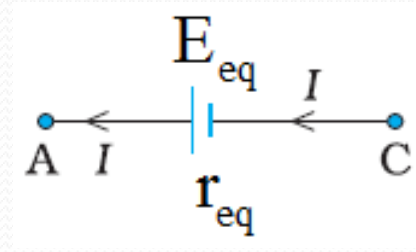
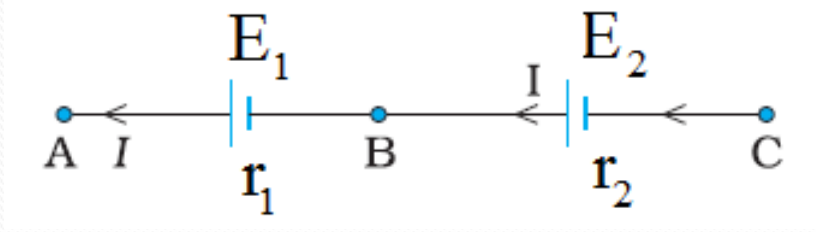
$$E = kl_1 = kl_{AN_1} = kl_1$$

$$V = E - Ir = kl_{AN_2} = kl_2$$

$$I = \frac{E}{R + r}$$

$$V = E - \frac{E}{R + r} r = \frac{ER}{R + r} = kl_2$$

$$\frac{R + r}{R} = \frac{l_1}{l_2} \Rightarrow r = R \left(\frac{l_1}{l_2} - 1 \right)$$



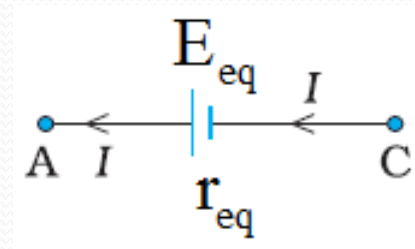
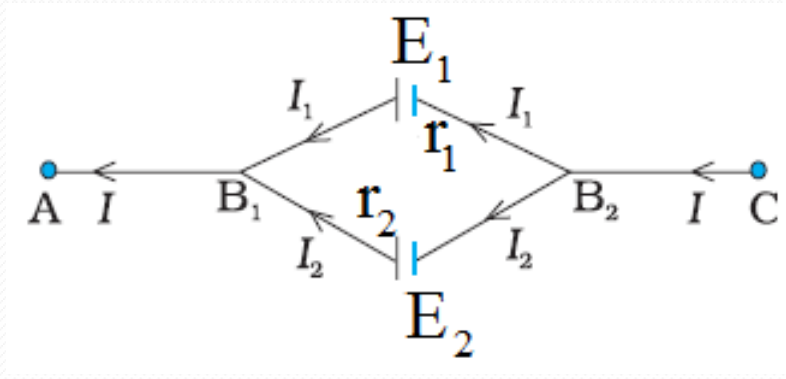
$$V_{AB} = E_1 - Ir_1; \quad V_{BC} = E_2 - Ir_2$$

$$V_{AC} = V_{AB} + V_{BC} = E_1 - Ir_1 + E_2 - Ir_2$$

$$V_{AC} = (E_1 + E_2) - I(r_1 + r_2)$$

$$V_{AC} = E_{eq} - Ir_{eq}$$

$$E_{eq} = E_1 + E_2 \quad \text{and} \quad r_{eq} = r_1 + r_2$$



$$V_{AC} = E_1 - I_1 r_1 = E_2 - I_2 r_2$$

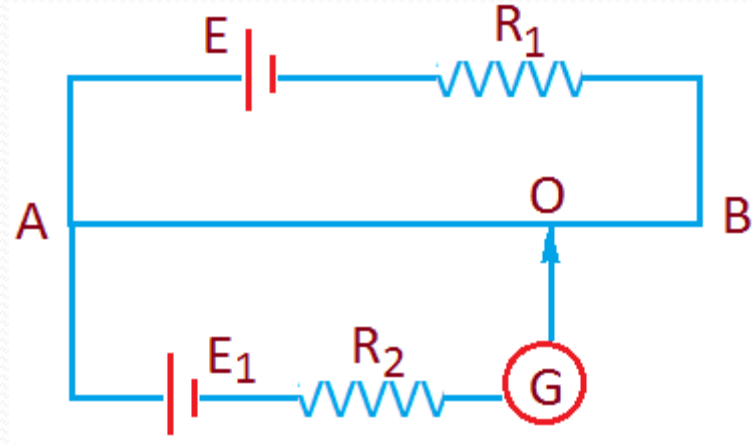
$$I_1 = \frac{E_1 - V_{AC}}{r_1} \quad I_2 = \frac{E_2 - V_{AC}}{r_2}$$

$$I = I_1 + I_2 = \frac{E_1 - V_{AC}}{r_1} + \frac{E_2 - V_{AC}}{r_2}$$

$$= \frac{E_1}{r_1} + \frac{E_2}{r_2} - V_{AC} \left(\frac{1}{r_1} + \frac{1}{r_2} \right)$$

$$\frac{E_{eq}}{r_{eq}} = \frac{E_1}{r_1} + \frac{E_2}{r_2}$$

$$\frac{1}{r_{eq}} = \frac{1}{r_1} + \frac{1}{r_2}$$



$$E = 20 \text{ V}, \quad R_{AB} = 20 \text{ } \Omega, \quad R_1 = 5 \text{ } \Omega, \quad R_2 = 5 \text{ } \Omega$$

$$L_{AB} = 200 \text{ cm}, \quad \text{Find AO}$$

$$(i) E_1 = 12 \text{ V} \quad (ii) E_1 = 18 \text{ V}$$

$$V_{AB} = ? \quad V_{AB} = IR_{AB} \quad I = \frac{20}{20+5} = \frac{4}{5} \text{ A}$$

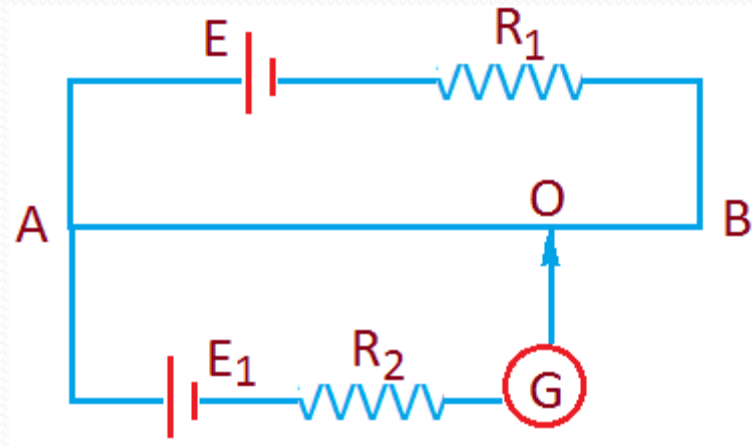
$$V_{AB} = \frac{4}{5} \times 20 = 16 \text{ V}$$

$$16 \text{ V} \equiv 200 \text{ cm} \Rightarrow 12 \text{ V} \equiv \frac{200}{16} \times 12 = 150 \text{ cm}$$

$$\text{Pot Gradient} = k = \frac{16 \text{ V}}{200 \text{ cm}}$$

$$12 \text{ V} = \frac{16 \text{ V}}{200 \text{ cm}} \cdot L \Rightarrow L = 150 \text{ cm}$$

$$18 \text{ V} = \frac{16 \text{ V}}{200 \text{ cm}} \cdot L \Rightarrow L = 225 \text{ cm}$$



$$E = 20 \text{ V}, \quad R_{AB} = 10 \ \Omega, \quad R_1 = 6 \ \Omega, \quad R_2 = 5 \ \Omega$$

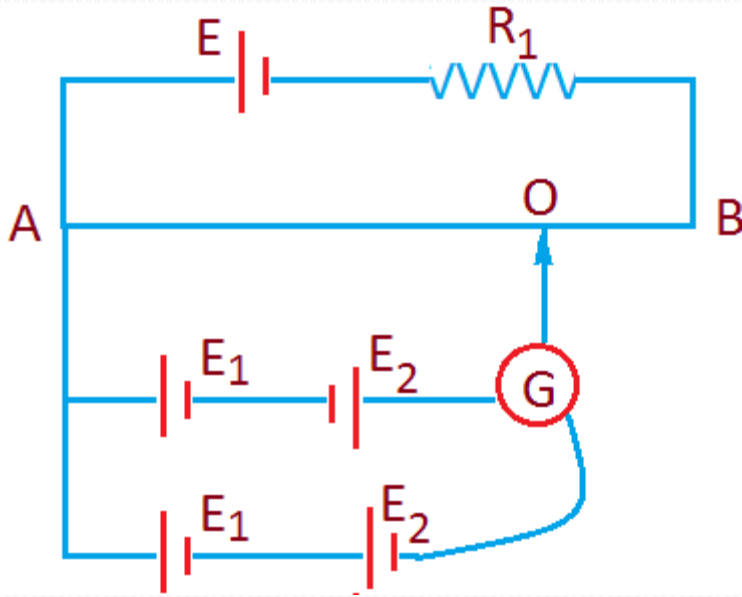
$$L_{AB} = 200 \text{ cm}, \quad AO = 40 \text{ cm} \quad \text{Find } E_1 ?$$

$$V_{AB} = IR_{AB} = \frac{20}{16} \times 10 = 12.5 \text{ V} \quad k = \frac{12.5}{200}$$

$$V_{AO} = kL_{AO} = \frac{12.5}{200} \times 80 = 5 \text{ V}$$

Find E , if $R_{AB} = 10 \ \Omega$, $R_1 = 6 \ \Omega$, $R_2 = 5 \ \Omega$, $L_{AB} = 300 \text{ cm}$, $AO = 60 \text{ cm}$ and $E_1 = 8 \text{ V}$.

$$k = \frac{8}{120} \quad V_{AB} = \frac{8}{120} \times 300 = 20 \text{ V} \quad I_{AB} = I = \frac{20}{10} = 2 \text{ A} \quad E = 2 \times 16 = 32 \text{ V}$$



In the figure, a long uniform potentiometer wire AB is having a constant potential gradient along its length. The null points for the two primary cells of emf's E_1 and E_2 connected in the manner shown, are obtained at a distance of 120 cm and 300 cm from the end A . Find (i) E_1 / E_2 and (ii) position of null point for the cell E_1

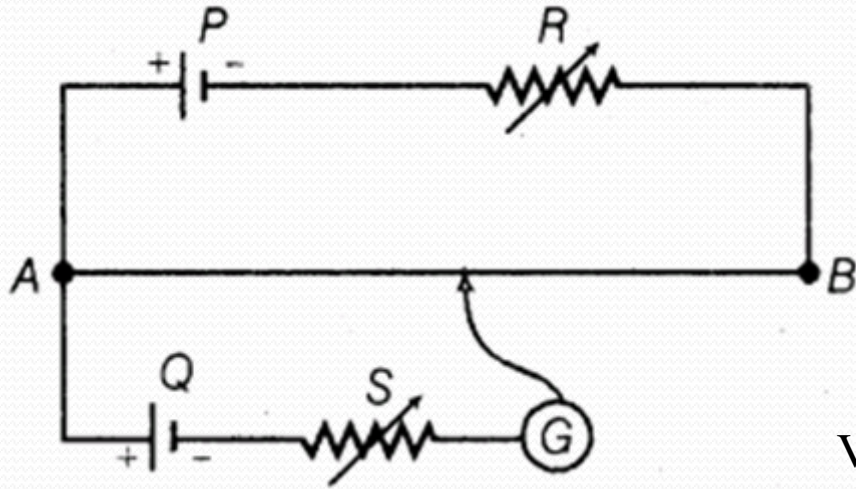
$$E_1 - E_2 = kl_1 = 120k$$

$$E_1 + E_2 = kl_1 = 300k$$

$$\frac{E_1 + E_2}{E_1 - E_2} = \frac{300}{120} = \frac{5}{2}$$

$$2E_1 + 2E_2 = 5E_1 - 5E_2 \Rightarrow 7E_2 = 3E_1 \Rightarrow \frac{E_1}{E_2} = \frac{7}{3}$$

$$E_1 + \frac{3}{7}E_1 = \frac{10}{7}E_1 = 300k \Rightarrow E_1 = 210k$$



Effect on balancing Length :

- (i) Resistance R is increased
- (ii) Resistance S is increased
- (iii) Length AB is increased
- (iv) Voltage of P is increased
- (v) Voltage of Q is increased
- (vi) Another R attached in parallel to R

$$V = kL; \quad k = \text{Potential Gradient}$$

$$k = \frac{V_{AB}}{L_{AB}} \quad V_{\text{BALANCE}} = \left(\frac{V_{AB}}{L_{AB}} \right) L_{\text{BALANCE}}$$

(iii) L_{AB} increase , L_{BALANCE} increase

(v) V_{BALANCE} increase , L_{BALANCE} increase

(i) V_{AB} decrease L_{BALANCE} increase

(ii) V_{AB} NO EFFECT L_{BALANCE} NO EFFECT

(iv) V_{AB} increase , L_{BALANCE} decrease

(vi) V_{AB} Increase , L_{BALANCE} Decrease