ELECTROSTATIC POTENTIAL

It is defined at a point ONLY like ELECTRIC FIELD

Work done in bringing a unit positive charge from infinity to that POINT against ELECTRIC force without ACCELERATION

$$V = \int_{\infty}^{r} \vec{F} \cdot d\vec{r} = \int_{\infty}^{r} F \cdot dr \cdot \cos 180^{\circ} = -\int_{\infty}^{r} F \cdot dr$$

$$F = k \frac{1 \times Q}{r^{2}} = k \frac{Q}{r^{2}}$$

$$V = -\int_{\infty}^{r} k \frac{Q}{r^{2}} \cdot dr = -kQ \int_{\infty}^{r} \frac{1}{r^{2}} \cdot dr$$

$$V = -kQ \int_{\infty}^{r} r^{-2} \cdot dr = -kQ \cdot \frac{r^{-2+1}}{-2+1} \Big|_{\infty}^{r}$$

$$V = -kQ \cdot \frac{r^{-2+1}}{-2+1} \Big|_{\infty}^{r} = kQ \left[\frac{1}{r} - \frac{1}{\infty} \right] = \frac{kQ}{r}$$

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$$W = \int_{\infty}^{r} \vec{F} \cdot d\vec{r} = \int_{\infty}^{r} F \cdot dr \cdot \cos 180^{\circ} = -\int_{\infty}^{r} F \cdot dr$$

$$F = k \frac{qQ}{r^{2}} = k \frac{qQ}{r^{2}}$$

$$W = -\int_{\infty}^{r} k \frac{qQ}{r^{2}} \cdot dr = -kqQ \int_{\infty}^{r} \frac{1}{r^{2}} \cdot dr$$

$$V = -kqQ \int_{\infty}^{r} r^{-2} \cdot dr = -kqQ \cdot \frac{r^{-2+1}}{-2+1} \Big|_{\infty}^{r}$$

$$W = -kqQ \cdot \frac{r^{-2+1}}{r^{2}} = kqQ \left[\frac{1}{r} - \frac{1}{\infty} \right] = \frac{kqQ}{r}$$

$$V = \frac{W}{q} = \frac{kQ}{r}$$